

Consider the curve defined by the equation  $2y^3 + 6x^2y - 12x^2 + 6y = 1$  with  $\frac{dy}{dx} = \frac{4x - 2xy}{x^2 + y^2 + 1}$

b) Write an equation of each horizontal tangent to the curve

$$4x - 2xy = 0$$

$$\frac{dy}{dx} = 0$$

$$2x(2 - y) = 0$$

$$2y^3 + 6y = 1$$

$$2x = 0 \quad 2 - y = 0$$

$$x = 0 \quad \text{and} \quad y = 2$$

c) The line through the origin with slope -1 is tangent to the curve at point P. Find the x and y-coordinates of P.

$$y = -x$$

$$\frac{4x - 2xy}{x^2 + y^2 + 1} = -1$$

d) Find  $\frac{d^2y}{dx^2}$  in terms of x and y.